

Problem Set 10: Torque, Rotational Dynamics, Physical Pendulum, Angular Momentum

Design Engineering Challenge: “The Big Dig” 2.007 Contest Paddle Spinning *Strategies*

PROBLEM 1:

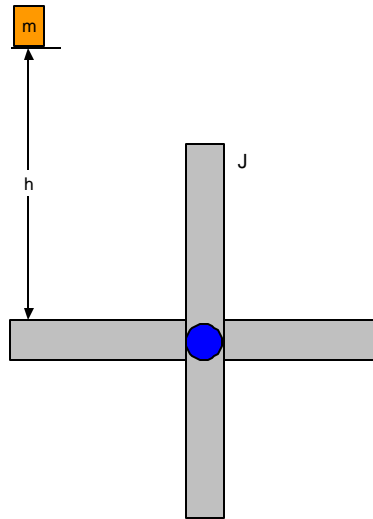


Figure 1: FBD of the two wheeled car

Conservation of Energy:

$$mgh = \frac{1}{2} J\omega^2 \Rightarrow \omega = \sqrt{\frac{2mgh}{J}}$$

Since $W = Fd = mgh$, $KE = \frac{1}{2} J\omega^2$

PROBLEM 2:

Height and/or mass of object can be increased to avoid an additional Force. To make it worth while, a substantial force must be added since angular velocity is proportional to the square root of work. $\omega \propto \sqrt{W} \Rightarrow$ To double angular velocity, force must be

quadrupled, $\omega = \sqrt{\frac{2W}{J}} \Rightarrow 2\omega = \sqrt{\frac{8W}{J}}$

PROBLEM 3:

The work above represents an elastic collision. Accounting for friction of the paddle wheel would reduce angular velocity.

PROBLEM 4:

Dropping the balls one after another maintains angular velocity, but does not increase it; it does not allow friction to bring the paddle to a stop. The terminal velocity is:

$$\omega = \sqrt{\frac{2mgh}{J}}$$

To increase angular velocity, more balls should be dropped together (at once):

$$\omega = \sqrt{\frac{2 \times (m_1 + m_2 + \dots + m_n)h}{J}}$$

In this case, angular velocity will be limited by the space between the paddles (i.e. how many balls can fit between paddles to increase angular velocity)

PROBLEM 5:

$$P = \Gamma \omega, T = FR = mgR, \omega = \frac{P}{mgR}$$

where,

m : mass of paddle

R : length of paddle

PROBLEM 6:

It is best to drop a heavy object into the mass scoring bin to and accelerate a hockey ball onto the paddle wheel to spin it up; since the angular velocity of the paddle is proportional to the square root of the work, it is not very advantageous to focus on increasing work.