

9(b) Employ N & mm units - hence stresses in MPa.
First select size then deduce corresponding A and I.

(i) size $\equiv A$, so $I = 0.15A^2$

(ii) size \equiv wall thickness, t
Let $D =$ outside diameter $= \tau t$
where τ is constant $= 15$

then $A = \frac{\pi}{4} [D^2 - (D-2t)^2] = \pi(\tau-1)t^2 = 14\pi t^2$

$I = \frac{\pi}{64} [D^4 - (D-2t)^4] = \frac{\pi}{8}(\tau-1)(\tau^2-2\tau+2)t^4$
 $= 137.9 \frac{\pi}{4} t^4$

(iii) size \equiv tabulated dimensions
A and I (note \bar{I}) from tables.

then proceed as follows:

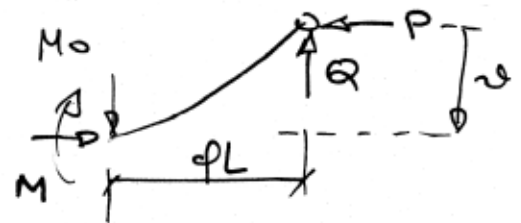
$\sigma_c = E(\pi/p)^2 = E(\pi/L)^2 I/A$
 $= 207 \times 10^3 (\pi/2400)^2 I/A$ MPa.

Hence solve (3), with $S = 250$, $\sigma_y = 60$ MPa, for $\bar{\sigma}$.
So $n = A \bar{\sigma} / F$ (where $F = 3 \times 10^5$ N) and compare
 n with specified value of 2.

	A mm ²	I mm ⁴	σ_c MPa	$\bar{\sigma}$ MPa	n	
(i)						
	4000	2.400×10^6	213	138	1.84	
	4200	2.646 "	223	143	2.00 \Rightarrow	
	4400	2.904 "	234	148	2.16	
(ii)						
	$t = 7$	2155	2.600 "	428	198	1.42
	8	2814	4.436 "	559	213	2.00 \Rightarrow
	9	3562	7.106 "	707	222	2.64
(iii)						
	22.9×76	3320	1.587 "	170	117	1.29
	89	4173	2.850 "	242	151	2.10 \Rightarrow
	25.4×76	3603	1.626 "	160	112	1.34
	89	4542	3.024 "	236	148	2.25

10. Take RH free body to eliminate central M_0 .

$M = P \cdot y + Q \cdot \phi L$
& $= -EI d^2 \psi / dx^2$
 $= -EI/2 \cdot d^2 \psi / d\phi^2$



So following analysis steps of notes:-

$d^2 \psi / d\phi^2 + \pi^2 \psi = - \frac{Q L}{P} \cdot \pi^2 \phi$

which has solution:

$\psi = A \sin \pi \sqrt{\phi} + B \cos \pi \sqrt{\phi} - \frac{Q L}{P} \phi$

cont'd