

where  $w_{ge}$  is the module of A-B-C & mde that of D-E  
 Substituting the geometric relations for  $r_p, r_e$  into the no-slip relations:-

$$\begin{aligned} z_A w_A &= \frac{1}{2} (z_A + z_C) w_2 + z_B w_B \\ z_C w_C &= \frac{1}{2} (z_A + z_C) w_2 - z_B w_B \\ z_E w_E &= [z_E - (z_C - z_A) z_D / 2z_B] w_2 - z_B w_B \end{aligned}$$

which, with  $w_e = 0$ , yields:-

$$w_E / w_A = [1 - z_C z_D / z_B z_E] / (1 + z_C / z_A)$$

- (a) If  $z_C z_D < z_B z_E$  then  $w_E / w_A > 0$ , i.e. both A & E rotate in same sense.

(b) Inserting values:  $w_E / 500 = (1 - 75 \times 19 / 60 \times 25) / (1 + 75 / 17)$

whence  $w_C = \frac{19}{1800} \times 500 = 4.62 \text{ rev/min.}$

If losses are negligible then  $P = w_1 T_1 = w_2 T_2$

i.e.  $T_E = 7.5 \times \frac{1}{5} \times 4.62 \times 60 \times \frac{1}{2\pi} = 15.5 \text{ kNm.}$

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Use the continued fraction technique:-

(i)  $1/\sqrt{2} = 0.70711 = 70711/100000$

70711 ) 100000 ( 1 = b<sub>1</sub>  
 70711  
 -----  
 29289 ) 70711 ( 2 = b<sub>2</sub>  
 58578  
 -----  
 12133 ) 29289 ( 2 etc  
 24266  
 -----  
 5023 ) 12133 ( 2  
 10066  
 -----  
 2087 ) 5023 ( 2  
 4174  
 -----  
 949 ) 2087 ( 2  
 1698  
 -----  
 389 ) 849 ( 2 etc.

n	0	1	2	3	4	5	6	7
b <sub>n</sub>	-	1	2	2	2	2	2	~3
A <sub>n</sub>	0	1	2	5	12	29	70	
B <sub>n</sub>	1	1	3	7	17	41	99	>120
C <sub>n</sub> = A <sub>n</sub> /B <sub>n</sub>	-	1	0.6667	.7143	.7059	.7073	.7071	
error * 10 <sup>4</sup>	-	-	-52	402	-17	+3	<1	

use 70:99.

(ii)  $\pi = 3.14159 \rightarrow 31416/10000$   
 since > 1, don't insert as above  
 10000 ) 31416 ( 3 = b<sub>1</sub>  
 30000  
 -----  
 1416 ) 10000 ( 7 = b<sub>2</sub>  
 9912  
 -----  
 88 ) 1416 ( 16  
 1408  
 -----  
 8 ) 88 ( 11  
 88  
 -----

n	0	1	2	3	4
b <sub>n</sub>	-	3	7	16	11
A <sub>n</sub>	0	1	7	113	
B <sub>n</sub>	1	3	22	355	
C <sub>n</sub>	-	3	3.1429	3.1416	
error * 10 <sup>4</sup>	-	-451	4	0	

Although the third convergent is accurate, the tooth numbers are unobtainable. Hence conclude that no solution possible.